

# Optimal Location of Transformers in Electrical Distribution Networks Using Geographic Information Systems

## *(Ubicación Óptima de Transformadores en Redes de Distribución Eléctrica Usando Sistemas de Información Geográfica)*

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### Abstract

*This research shows a heuristic model for the design of scalable and reliable electrical distribution networks. The algorithms presented allow to optimize the location of transformation centers using on their database geographic information systems from which it is possible to define user locations, candidate sites, possible routes for the deployment of the electricity grid and, in general, data for the reconstruction of the scenario. The model employs clustering and triangulation methods, as well as algorithms for creating a minimally expanding tree and the consequent site assignment for transformer placement. After setting the optimal locations for the transformer site, the algorithms compute voltage drops in secondary circuits, required transformation capability, execution times, and coverage achieved. The results obtained are adjusted to the requirements of an actual distribution power grid and show a good performance on the proposed scenario.*

### Keywords

*Optimal deployment; sizing; planning; transformation centers.*

### Resumen

La presente investigación muestra un modelo heurístico para el diseño de redes de distribución eléctricas escalables y confiables. Los algoritmos presentados permiten optimizar la ubicación de centros de transformación usando sobre su base de datos sistemas de información geográfica de las cuales es posible definir ubicaciones de usuarios, sitios candidatos, posibles rutas para el despliegue de la red eléctrica y en general, datos para la reconstrucción del escenario. El modelo emplea métodos de clusterización y triangulación, así como algoritmos para la creación de un árbol de mínima expansión y la consecuente asignación de sitios para la ubicación de transformadores. Tras establecer las ubicaciones óptimas para el emplazamiento de unidades, los algoritmos determinan caídas de voltaje en circuitos secundarios, capacidad de transformación requerida, tiempos de ejecución y cobertura alcanzada. Los resultados obtenidos se ajustan a los requerimientos de una red eléctrica de distribución y muestran un buen desempeño sobre el escenario propuesto.

### Palabras clave

Despliegue óptimo; dimensionamiento; planificación; centros de transformación.

## 1. Introduction

This research is an extension of the article titled "Optimal Allocation of Transformers in Electrical Distribution Systems Considering Attenuation and Capacity Constraints", previously presented at the 4th INCISCOS 2019 International Conference held in the city of Quito - Ecuador.

Traditional electrical networks become smart grids if communications infrastructure is added, some researches about technologies are described considering optimal communications and infrastructure in HAN (Maldonado, 2017), NAN (Quishpe, Padilla & Ruiz, 2019; Ruiz, Masache & Inga, 2018; Ruiz Maldonado & Inga, 2019) and WAN (Ruiz & Inga, 2019; Ruiz, Masache & Domínguez, 2018).

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Distribution systems play an essential role since it interconnects the transmission system and the users. Research efforts in the area have been directed toward developing methodologies for optimal design, planning, and expansion of modern electrical distribution systems (Carrión Galarza & González Sánchez, 2019).

Traditional design methodologies must minimize the associated costs, such as investment, energy losses, operation and maintenance while keeping satisfactory levels of security and reliability. Information about the electrical distribution network, such as location and ratings of generators, substations, transformers and lines, and the electric energy demand of the users is key for solving this optimization problem. However, publicly available data from a real network is generally scarce. Therefore, considering the demand increase, when planning distribution networks, typically requires the use of artificial models that emulate the real infrastructure. The optimal design of smart distribution networks is a combinatorial problem defined as NP-complete, next papers show different methodologies for design electrical networks (Liu et al., 2017; Xie et al., 2018); where the connection between customers and the main node on a georeferenced scenario is build using a model based on minimum spanning tree (MST) techniques.

The project deals with the optimal location of distribution transformers using a modified-prim algorithm based on the minimal cost of low voltage network between transformers and users. Secondly, clustering algorithms are used to break the dataset (number of distribution transformers) up into groups, then the k-medoids algorithm determines a defined number of clusters, which can be used as primary feeders. The next stage deals with the built-up of the medium voltage network based on modified-prim (Gholizadeh-Roshanagh, Najafi-Ravadanegh & Hosseinian, 2018; Xie et al., 2018) to determine the lowest path between the main substation and distribution transformers on a georeferenced path. The minimum spanning tree (Li, Mao, Zhang & Li, 2016) is estimated with the Prim algorithm and graph theory. Prim is used to finding the subset of branches and all vertices that will constitute the tree. The constraint related to the losses due to distances is taken into account during the process. In each iteration, the algorithm increases the tree size, starting from an initial vertex representing a transformer and successively adding vertices corresponding to the users, such that the distances between the transformer and the users are minimized, initial works in telecommunications. This process considers variables such as location of the householders' main feeders, location, and ratings of transformers and path of medium and low voltage along the streets; it also takes into account constraints such as power flow balance/equality, the location of a substation, the path of lines, bus voltage and ratings and coverage of each transformer. Regarding the latter, any transformer that does not satisfy the requirements is to replace. The proposed model in this paper is to develop considering a multigraph, that defines a layer for the medium voltage network and another layer for the low-voltage network, ensuring the connectivity of users in the deployment depending on demand. To achieve the objectives a deployment is carried out in urban areas using an open street map (OSM) (Once, 2017) file with the information of longitude and latitude within a model developed in Matlab. The efficiency of the model is estimated for varying densities of the electric load, to assess adaptation capability and resources available to fulfill the demand of a different number of users. The k-means algorithm is used for generating the clusters, and the nodes inside an area are treated as PQ loads. Such a network is generated through the Delaunay-Voronoi triangulation (Budka, K., Deshpande, J. and Thottan, 2014; Ciechanowicz, Pelzer, Bartenschlager, & Knoll, 2017), thus resulting in a partially connected mesh. If such mesh network shows a redundancy larger than desired, branches are iteratively suppress starting with the one connecting two nodes with the highest degree.

Henceforth, this article is organized as follows. Section 2 presents the methodology of the problem, where the proposed algorithms and procedures for optimization are formulated. Section III presents results and discussion, describing and analyzing the information obtained by applying the optimization model on simulation scenarios with different parameters. Finally, in section V, the conclusions and recommendations about this research.

## 2. Methodology

Planning electrical distribution networks involves, among other aspects, taking some initial considerations that allow defining preliminary parameters to their implementation on the optimization model. The considerations included in the research respond to the deployment of a new power grid. This implies that existing distribution network is not considered, or in turn, it does not exist. Items considered, such as location of users, candidate sites and possible routes for the deployment of the electricity network, are identified using georeferenced data from the OpenStreetMap platform after their processing in MATLAB. In addition to characterization of the scenario, the object of the implementation of georeferenced information lies in the ability to facilitate the obtaining of coordinates where the location of the electrical transformers is adequate. Being this, one of the results obtained through the model presented. Table 1 shows the variables of equations and algorithms shown later.

**Table 1.** Variables and notation

Nomenclature	
$X, Y$	Array of user and candidate sites locations, respectively.
$\zeta_k$	State variable of the $k$ -th candidate site.
$\psi^{min}$	Minimal spacing constant between transformers.
$\xi$	Distance between each of the active transformers.
$P_U$	Demand from each user.
$\lambda$	Maximum transformation capability.
$\gamma$	Number of regions for clustering.
$m^{idx}, m^{xy}$	Index assigned to each user and medoid locations, respectively.
$MP_U$	Vector of demand assigned to each user.
$\phi$	Graph obtained by applying the Prim algorithm.
$\vartheta$	Preliminary array of logical values of active sites and assigned users.
$\beta$	Transformer(s) assigned to a user
$\mathcal{S}$	Coordinates for the transformer location.
$\rho_c; S_c$	Resistivity and cross-section of the conductor.
$\mu$	Set of users assigned to a transformer.
$P_{tfo}$	Transformer power.

$d_U^s$	Distance between the user and their assigned transformer.
$R, I$	Resistance and current along the section between transformer and user's meter
$v_L, \varphi$	Line voltage and estimated power factor over the secondary circuit
$\nabla V$	Voltage drops of secondary circuits.

Being  $N$  the number of users and  $M$  the number of candidate sites, it is sought to minimize the number of candidate sites considering the spacing between transformation centers, and their maximum capability; which must be greater than the sum of the power demanded by users connected to the equipment, ensuring that the specified transformability will not be exceeded. The mathematical expressions that respond to the above are presented below, being (1) the objective function, (2) spacing restriction and (3) maximum transformation capability restriction.

$$\text{Min: } \sum_{k=1}^M \zeta_k; \zeta \in \{0, 1\} \quad (1)$$

$$\psi^{min} < \xi \quad (2)$$

$$\sum P_U \leq \lambda; \forall U / \{U: U \in \text{coverage}(Tfo)\} \quad (3)$$

Once the scenario is characterized and after defining the candidate sites for the location of transformers, taking into account the characteristics of the design area; a scenario where a large number of users are available could involve excessive complexity to perform optimization in large blocks, so it is chosen to cluster the design area in a way that makes routing easier by creating subnets. Sectorization is done using the k-medoids clustering method, thus dividing the environment into regions while building a graph connecting the different nodes in the geo-referenced area. The clustering result is also used for assigning random loads to each user. Also, Delaunay and Voronoi triangulation methods are used to visualize sectorization. After that, it is proposed to solve the problem of optimal location using the modified-Prim and Greedy algorithms. The above process is carried out when applying Algorithm 1.

**Algorithm 1:** Clustering and Optimal Location of Electrical Transformers

1:	<b>procedure</b> Input( $X; Y; N; M, \gamma, \psi^{min}, \lambda$ )
2:	<b>Step 1:</b> Create subregions
3:	$[m^{idx}, m^{xy}] = kmedoids(X, \gamma)$
4:	$t^d = delaunay(m^{xy}(:,1), m^{xy}(:,2))$
5:	$voronoy(m^{xy}(:,1), m^{xy}(:,2), t^d)$
6:	<b>Step 2:</b> Random demand assignment
7:	$MP_U = random; \forall U / \{U: U \in m_k^{idx}\}$
8:	<b>Step 3:</b> Modified Prim Algorithm

9:	$\phi = \text{prim}(X, Y, \psi^{\min}, \lambda)$
10:	<b>Step 4:</b> Greedy-SCP
11:	$\vartheta = \text{greedyscp}(\phi)$
12:	<b>Step 5:</b> Eliminate redundancy
13:	for $i = 1$ to $N$ do
14:	$\beta = \text{find}(\vartheta(i, :) == 1)$
15:	if $\text{length}(\beta) > 1$ then
16:	for $j = 2$ to $\text{length}(\beta)$ do
17:	$\vartheta(i, \beta(j)) = 0$
18:	end for
19:	end if
20:	end for
21:	<b>procedure</b> Output( $MP_U, \vartheta$ ) <sup>w</sup>

From Algorithm 2, modified-Prim method allows building a minimum expansion tree over the network. The graph obtained includes all the vertices of the network where the sum of its edges is minimum, the weights of the graph are the distances between users and candidate sites obtained by the haversine formula. On the other hand, the Greedy algorithm allows obtaining an array with logical values that show those active transformers that will meet the demand of the different user blocks. However, the array of logical values obtained with Greedy can present minor problems, such as providing a solution that includes more than one transformation unit for the same user, which would result in incorrect transformer sizing and, in general, unwanted redundancy errors. Therefore, the algorithm considers that particularity and corrects it.

The procedure implemented by Algorithm 2 allows determining the capability of the transformers and after the nominal power of each transformer has been obtained, the algorithm performs a calculation of the existing distances for the set of users covered by a transformer using the haversine formula, this procedure is applied to the full extent of the distances between a user and its assigned transformer; with this data, voltage drop calculations are performed based on the parameters of the established conductor, as well as electrical factors typical of the network and demand, such as voltages in secondary and power factor.

**Algorithm 2:** Sizing and voltage drops in secondary circuits calculation

1:	<b>procedure</b> Input( $\mathcal{S}; \rho_c; s_c; N; M, \gamma, \psi^{\min}, \lambda$ )
2:	<b>Step 1:</b> Transformer sizing
3:	for $i = 1$ to $\text{length}(\mathcal{S})$ do
4:	$\mu = \text{find}(\vartheta(:, i) == 1)$
5:	$s_p = 0$

6:	for $j = 1$ to $length(\mu)$ do
7:	$s_p = s_p + MP_U(\mu(j))$
8:	end for
9:	$P_{tfo}(i) = s_p$
10:	end for
11:	<b>Step 2:</b> Calculate distances
12:	$d_U^S = haversine(X, S); \forall U/\{U: U \in coverage(Tfo)\}$
13:	<b>Step 3:</b> Calculate voltage drops
14:	for $i = 1$ to $length(P_{tfo})$ do
15:	$R(i) = d_U^S \times (\rho_c \div s_c)$
16:	$I(i) = P_{Tfo}(i) \div (v_L \varphi)$
17:	$\nabla V(i) = R(i) \times I(i)$
18:	end for
19:	procedure Output( $P_{tfo}, \nabla V$ )

### 3. Results and Discussion

MATLAB R2018b software is used to implement the proposed methodology on a computer with an Intel Core i7-6500U processor, 8 Gb of RAM, and Windows 10. The proposed scenario has 824 users and 163 candidate sites located at the intersections of the georeferenced area, obtained after recognition by interpreting geographical information. The proposed georeferenced area is shown in Figure 1, along with the location of the candidate sites, users and clustering of the area.

**Figure 1.** Proposed georeferenced area with the location of candidate sites and users.

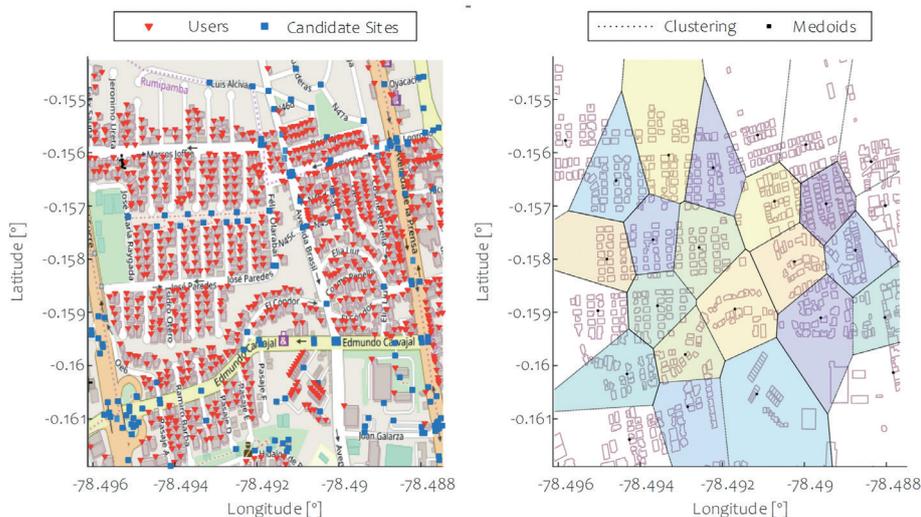


Table 2 shows results achieved after applying the optimization methodology on the proposed scenario. In order to obtain these values, the spacing and maximum transformation capability parameters considered were 100 meters and 200 KVA, respectively.

As can be seen, 18 active sites are obtained, which refer to the set of coordinates marked by the model as optimal to the location of transformation centers. The number of active sites represents eleven percent of the total available sites. On the other hand, while the set of transformation units to be deployed on the network does not guarantee a total supply of demand, since the coverage is not 100 %; the number of users not supplied is minimal, so they could be assigned to a transformer with low loadability. In this sense, the table also shows information about the maximum and minimum number of users assigned to a transformer. This data shows the condition of certain units in which the number of users is minimal, so they can withstand higher load and therefore will be able to supply the entire demand.

**Table 2.** Summary of parameters obtained after applying the optimization methodology

Parameter	Obtained Value
Number of active sites	18
Number of users	804
Electric coverage [%]	97.573
Maximum number of assigned users	153
Minimum number of assigned users	1

Figure 2 shows the georeferenced area with the deployment of the transformation units located at the coordinates rated as optimal. In addition, the primary of the electrical network covering each of the active transformation units is shown. This network constitutes a possible route for the deployment of the power grid.

**Figure 2.** Optimal allocation of transformers in the georeferenced area and deployment of the feeder

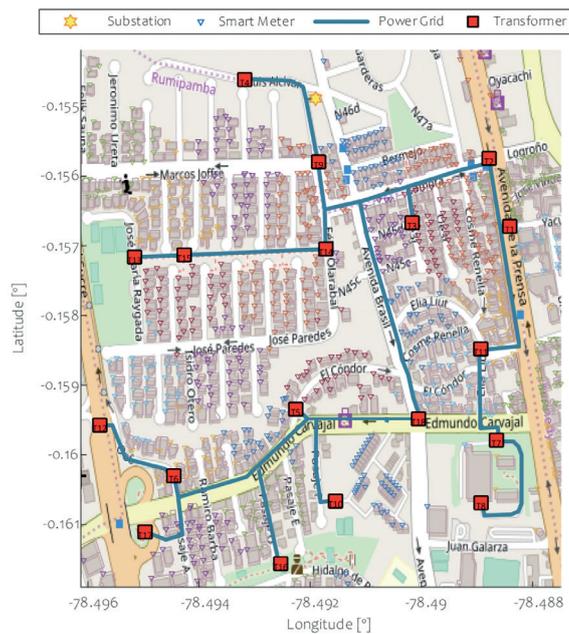


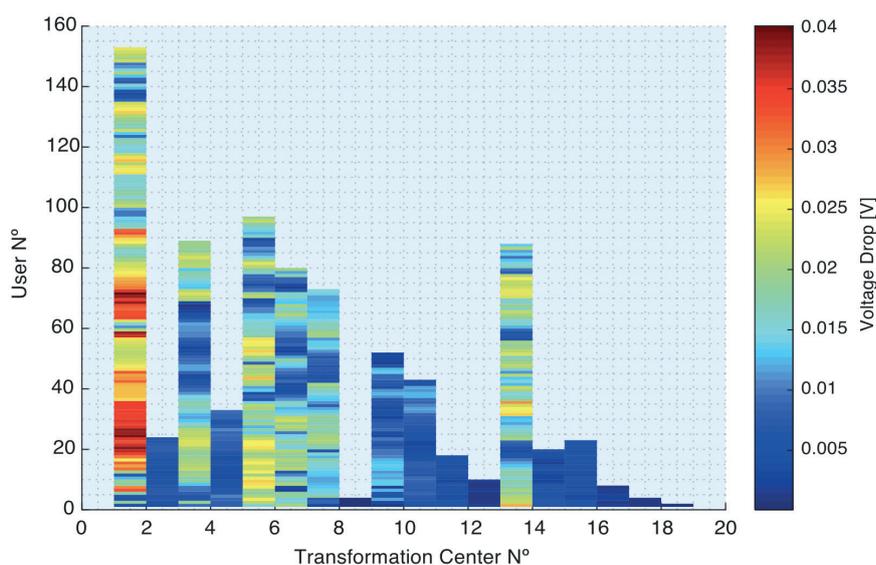
Table 3 shows the capability of each transformation unit located in the georeferenced area. Values presented are based on standard values. The maximum capability obtained after sizing reaches 150 KVA in a single unit, ensuring compliance with the maximum capability constraint.

**Table 3.** Power capability of the transformation units

Transformer	Power [KVA]	Transformer	Power [KVA]	Transformer	Power [KVA]
T1	150	T7	75	T13	100
T2	30	T8	15	T14	30
T3	100	T9	75	T15	30
T4	50	T10	50	T16	15
T5	100	T11	30	T17	15
T6	100	T12	15	T18	15

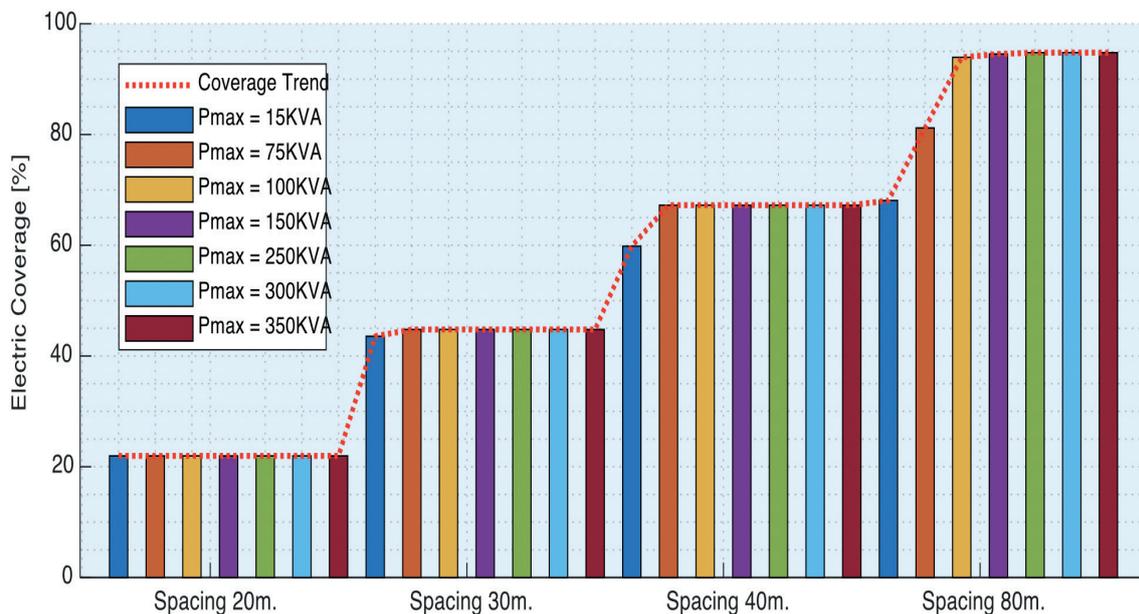
Voltage drops, corresponding to the secondary circuits of the network, cover the sections between each user and its assigned transformer. Figure 3 shows these drops obtained by using the following parameters: voltage 120 volts, power factor 0.85 and 1/0 aluminum conductor. Thus, the maximum voltage drop would be around 0.04 volts, which is 0.033 % of the total voltage. However, most users would have drops ranging from 0.01 to 0.025 volts. Consequently, it can be said that the expected voltage attenuation should not violate the standards for distribution systems. Voltage drops are calculated only in secondary circuits due to the model handles user and active transformer locations. So, with such parameters, it is possible to calculate distances and therefore voltage drops between users and their assigned transformer. The voltage drop in primaries is not addressed since the model does not perform optimal network routing. In addition, Figure 3 shows the distribution of users for each of the active transformers, providing an overview of the coverage of each transformer. Furthermore, the maximum and minimum number of users connected to a transformer is appreciated, in accordance with data shown above in Table 2.

**Figure 3.** Voltage drops in secondary circuits for the proposed scenario



Another aspect to be evaluated is the percentage of electrical coverage achieved after the location of the transformation centers. Since no coverage constraints are introduced, this parameter is not controlled, however, the results achieved expose a marked trend. Figure 4 shows coverage values obtained after applying the optimization methodology considering changes in the restrictive parameters of the model. The minimum coverage values are placed when using as the spacing distance of 20 meters. For this distance, even when the maximum transform capability changes, coverage remains fixed at approximately 22 %. Similarly, it occurs for spacing values of 30 and 40 meters, with coverage values of 45 % and 67 %, respectively. For spacing values of 80 meters, coverage improves considerably, except for results obtained for powers less than 100 KVA, the coverage reaches approximately 95 %.

**Figure 4.** Network coverage by variations in model restrictions



Following the trend, coverage below the tested minimum distance is expected to be low and above the maximum distance tested would be greater than 95 %. However, the distance parameters used as constraints do not fit the needs of an actual distribution system. Since even the distance between poles should be commonly greater than 40 meters. Even, as a minimum spacing a distance less than that value, involves violating the minimum distance requirement between posts and, considering a spacing value equal to 40 meters, would imply the possibility of placing a transformer on each post, which nor does it fit the reality. Generally, transformers are located at distances of not less than 100 meters and as presented above, the coverage achieved under that distance is around 96 %.

**Figure 5.** Execution times resulting from variations in spacing and transformation capability

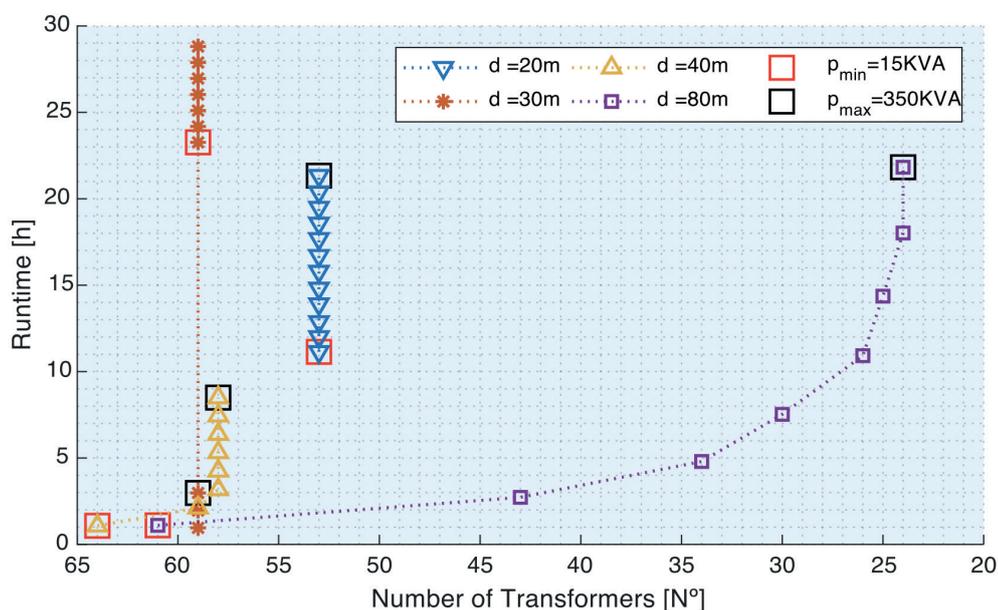


Figure 5 shows data regarding execution times as a result of applying the optimization methodology and the variation of its restrictions. It should be noted from this figure that the markers refer to the maximum and minimum powers used for the creation of the different scenarios, which correspond to 350 KVA and 15KVA, respectively. These values correspond to the power horizons used, however, among these values there are more power parameters. Having said that, it can be observed that for a spacing of 20 meters all the results obtained yield the same asset site numbers, specifically, 53. Although the number of active transformes is the same, execution times experience an increase, starting from 11 hours, for the minimum horizon, to 21 hours, on the maximum horizon. Similarly it happens with the spacing of 30 meters, obtaining a number of active sites of 59, in this case the execution time presents a decrease, so the maximum execution time is 29 hours and the minimum 1 hour. For the spacing of 40 meters, different numbers of active sites were obtained, starting with 64 to reach 58 active sites, with times ranging from 1 hour to 9 hours, being that, in the same way, there is an increase in the execution time. Finally, with the spacing of 80 meters, different numbers of active sites were obtained forming a growing curve in time and decreasing in number of transformers. In the latter, times range from 1 hour to 22 hours.

## 5. Conclusions and Recommendations

The optimization methodology presented uses georeferenced information for the characterization of the scenario. It includes identifying users, candidate sites, and possible routes for network deployment. This work considers the deployment of a new power grid and the model does not identify or consider existing networks. So, in a scenario where a network is already deployed, the results can help assess whether the current location of the transformation units is adequate and if it is not, to consider the relocation of the transformer, this, accompanied by specific analyses as economic implications.

Voltage drops achieved do not exceed the typical maximum permissible values stipulated by regulations for electrical distribution systems. The resulting values show an adequate location of the transformers, as their reduced magnitudes respond to a well-achieved proximity between users and their assigned transformer, this implies that the distance between them is small and as a result, little attenuation is achieved.

Assignment of users to each transformation unit is not uniform, presenting cases in which a transformation unit covers just a single user. This is justified in cases where the user has a high electrical demand. And even if the above does not stick to reality, such units can be considered in the expansion of the distribution system.

The coverage obtained in scenarios with spacings less than 80 meters is limited, however, the use of such parameters is not applicable to the requirements of a distribution network, since, as explained during the analysis, some of these values involve the possibility of placing transformers on each of the poles in the distribution network. With spacings greater than 80 meters the coverage reaches quite acceptable levels, above 95 %. Despite achieving acceptable levels for certain ranges, future research should include coverage restrictions to ensure full demand supply, even if the restrictions do not adhere to the actual requirements of a distribution network.

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